

ANSWER KEY FOR CLASS 10.

EX – 6 Factorisation

2.i) Since $x+3$ is a factor of $f(x)$ by remainder theorem, $x+3 = 0$ or $x = -3$.

$$f(x) = 2x^2 - 5x + 4 = 2x(-3)^2 - 5x(-3) + 4 = 18 + 15 + 4 = 37 \text{ ans.}$$

5. Since $x-2$ is a factor of $f(x)$, by remainder theorem, $x-2=0$ or, $x = 2$.

$$f(x) = 2x^3 + 3x^2 - kx + 5 = 7 \text{ or, } 2x^3 + 3x^2 - kx + 5 = 7 \text{ or, } 16 + 12 - 2k + 5 = 7 \text{ or, } x = 13.$$

8ii) Since $x+3$ is a factor of 2 polynomials, by remainder theorem, $x+3=0$ or $x=-3$

$$f(x) = ax^3 + 3x^2 - 9 = a(-3)^3 + 3(-3)^2 - 9 \dots (1) \text{ also, } g(x) = 2x^3 + 4x + a = 2(-3)^3 + 4(-3) + a \text{ by}$$

the problem, $-27a + 18 = -66 + a$ or, $28a = 84$ or, $a = 3$ ans.

$$16i) f(x) = 2x^3 + x^2 - 13x + 6 \text{ when } x=1/-1/2 \text{ then } f(x) \neq 0 \text{ when } x=2 f(x) = 0$$

therefore, by factor theorem, $x-2$ is a factor. Now, by simple division

$$2x^3 + x^2 - 13x + 6 \div x-2 \text{ we get } 2x^2 + 5x - 3. \text{ Again by factorisation we get } (x+3)(2x-1).$$

Ans. 22. Since $x-2$ is a factor of $f(x)$, by factor theorem, $x-2 = 0$ or, $x = 2$

$$f(x) = x^3 + ax^2 + bx - 12 = 0 \text{ or, } 2^3 + a \cdot 2^2 + b \cdot 2 - 12 = 0 \text{ or, } 2a + b = 2 \dots (1)$$

.Again, since $x+3$ is a factor, by factor theorem, $x+3=0$ or, $x=-3$.

$$f(x) = (-3)^3 + a(-3)^2 + b(-3) - 12 = 0 \text{ or, } 3a - b = 39 \dots (2). \text{ Solving, we get } a=3, b=-4.$$

CHAPTER TEST

1. Since, $2x+1$ is a factor, by factor theorem, $2x+1=0$ or, $x=-1/2$

$$f(x) = 2x^3 - 3x^2 + 4x + 7 = 2(-1/2)^3 - 3(-1/2)^2 + 4(-1/2) + 7 = 4 \text{ ans.}$$

3. Since, $2x-3$ is a factor, by factor theorem, $2x-3=0$ or, $x = 3/2$

$$f(x) = 6x^2 + x + a = 0, \text{ or, } 6(3/2)^2 + (3/2) + a = 0 \text{ or, } a = -15.$$

On simple division $6x^2 + x - 15 \div 2x - 3$ we get $(2x-3)(3x+5)$. Ans.

6ii) $f(x) = x^3 - 19x - 30$. putting $x = 1/-1/2$ $f(x) \neq 0$ but when $x=-2$, $f(x) = 0$. so, $x+2$ is a factor. By simple division $x^3 - 19x - 30 \div x+2$ we get $x^2 - 2x + 5$. again by factorising we get $(x+3)(x-5)$. So, $(x+2)(x+3)(x-5)$ are the factors.

8. Since, $x+3$ is a factor, by factor theorem, $x+3=0$ or, $x=-3$.

$$f(x) = x^3 + ax^2 - bx + 24 = 0 \text{ or, } (-3)^3 + a(-3)^2 - b(-3) + 24 = 0 \text{ or, } 3a + b = 1 \dots (1)$$

also, since, $x-4$ is a factor, by factor theorem, $x-4=0$ or, $x=4$.

$$f(x) = x^3 + ax^2 - bx + 24 = 0 \text{ or, } 4^3 + a \cdot 4^2 - b \cdot 4 + 24 = 0 \text{ or, } 4a - b = -22 \dots (2).$$

On solving $a=-3, b=10$. Therefore, $f(x) = x^3 - 3x^2 - 10x + 24$. Now, by simple dividing $x^3 - 3x^2 - 10x + 24 \div x-4$, we get $x^2 + x - 6$. again, by factorising we get $(x+3)(x-2)$. Therefore, $(x-4)(x+3)(x-2)$ are the factors.

10. Since $2x+1$ is a factor, by factor theorem, $2x+1=0$ or, $x=-1/2$. putting $x=-1/2$ in two $f(x)$ and solving we get $p=-3, q=2$. by factorising, $x+2, x-3$.

